#### Composite Dark Matter from Sp(2N) gauge theories



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mostly based on 2202.05191, 2304.07191, 2311.18549

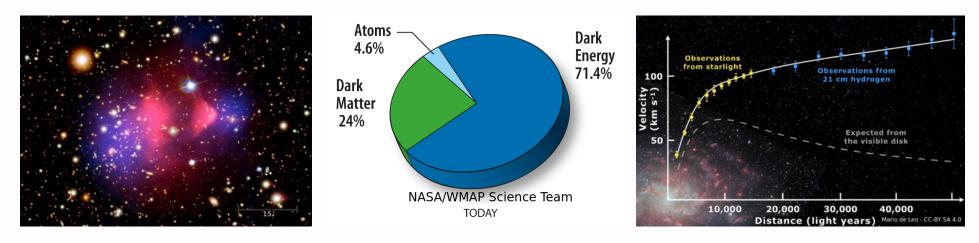
slides available at: fzierler.github.io/talks/

#### Outline

- Composite, self-interacting Dark Matter models
  - Strongly Interacting Massive Particles (SIMPs)
  - $\circ$  A specific model: Sp(4) with two Dirac fermions
- Lattice Field Theory and numerical results
  - Meson spectroscopy
  - Goldstone scattering
  - Conclusions for Phenomenology and model building

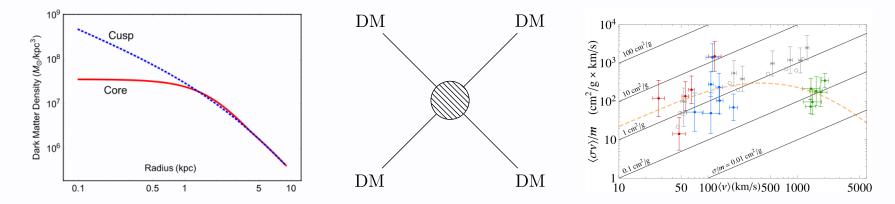
#### Dark Matter - Why?

- Strong observational evidence at many scales! <sup>[1]</sup>
- Modified Gravity <sup>[2]</sup> is a potential alternative
- New particles beyond the Standard Model (BSM) promising!



#### [1] see e.g. Bullock, Boylan-Kolchin [1707.04256], Tulin, Yu [1705.02358] Dark Matter properties

- DM self-interaction phenomenologically allowed<sup>[1]</sup> and potentially relevant for small-scale structure problems
  - $\circ$  non-vanishing scattering cross-sections  $\sigma_{
    m 2DM 
    ightarrow 2DM}$
  - $\circ$  velocity dependence of  $\sigma_{
    m 2DM 
    ightarrow 2DM}$  preferred



QCD-like Dark Matter can those provide self-interactions!

#### Strongly Interacting Gauge Theories in DM Models

- With fermions: Global symmetries make DM stable
- With mediator: Dark sector coupled to SM

$$\underbrace{\mathrm{DM}}_{\mathrm{M}} \underbrace{\mathrm{M}}_{\mathrm{M}} \underbrace{\mathrm{M}} \underbrace{\mathrm{M}} \underbrace{\mathrm{M}}_{\mathrm{M}} \underbrace{\mathrm{M}} \underbrace{\mathrm{M} \underbrace{\mathrm{$$

• Non-vanishing self-scattering cross-section arise

$$\langle v \sigma_{\pi\pi o \pi\pi} 
angle 
eq 0$$

• Relic density driven by strong processes

#### Dark meson scattering: Determine DM relic density

• Any model must predict the current density of DM correctly  $\circ$  number density n can be calculated using Boltzmann equations

$$\partial_t n + 3Hn = f(\langle v\sigma_{ ext{number changing}} \rangle)$$

- Cross-sections  $\langle \sigma v 
  angle$  are input for Boltzmann equations
  - describe non-equilibrium dynamics
  - $\circ~H$  is the Hubble rate

#### Strongly Interacting Massive Particles (SIMPs)

- Depletion via  $3{
m DM} o 2{
m DM}$   $^{[1]}$ , i.e.  $3\pi o 2\pi$ 

 $\circ$  same as  $KK 
ightarrow 3\pi$  in QCD  $^{[2]}$ 

• Dark matter depletion process: *freeze-out* 

- LO ChiPT matches relic density at $m_\pi pprox {\cal O}(100){
  m MeV} {\cal O}(1){
  m GeV}$
- Other mass scales than QCD are relevant!

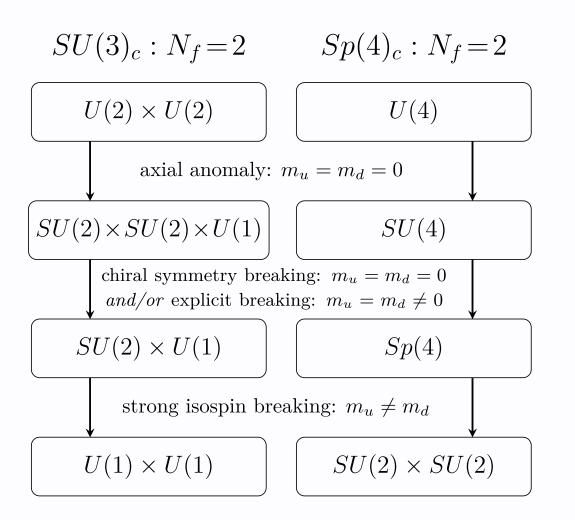
 $\circ~g^2$  and  $m_f$  are free parameters

Dark Matter with 3DM  $_{\rightarrow}$  2DM depletion and self-interactions

[1] Hochberg et. al. [1411.3727] [1512.07917] [2] Choi et.al. [1801.07726] Bernreuther et.al. [2311.17157]
 [3] Kulkarni et.al. [2202.05191] [4] Chu et.al. [2401.12283] Kondo et.al. [2205.08088]

#### Other relevant channels

- decay to Standard Model:  $2\pi o SM$   $^{[1]}$
- involvement of vector mesons:  $\pi\pi o \pi
  ho$  ,  $3\pi o \pi
  ho$   $^{[2]}$
- influence of light singlets:  $\eta'\eta' o \pi\pi, \pi\pi o \eta'\pi$ ,  $\dots$   $^{[3]}$
- ullet resonances and multi-hadron states:  $2\pi o 2\pi$  ,  $2n\pi o 2\pi$   $^{[4]}$
- The relevance depends on the spectrum
- lattice investigations inform EFT construction



#### SIMPs from Sp(4) gauge theory

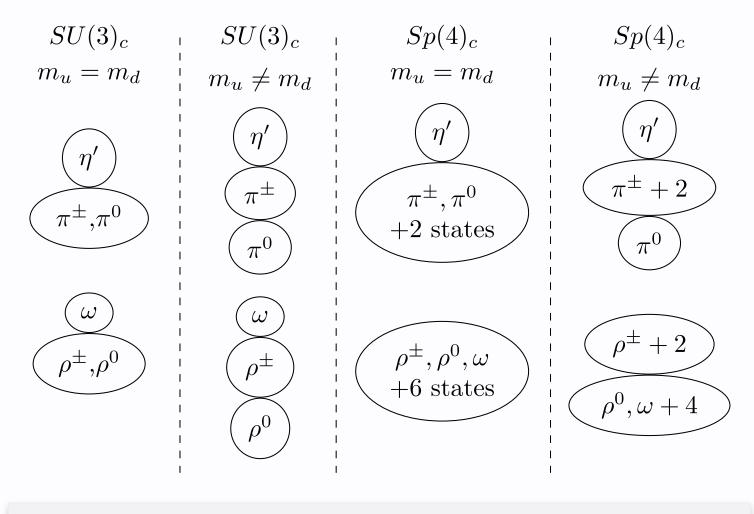
Pseudo-real representation: <sup>[1]</sup>
 ⇒ more pseudo-Goldstones

 $\Rightarrow$  no fermionic bound states

•  $N_f=2:$  exactly 5 Goldstones  $\circ$  Allows  $3{
m DM}
ightarrow 2{
m DM}$   $^{[2]}$ 

Sp(4) with two fermions is a minimal SIMP DM realisation

### Meson multiplets of $Sp(4)_c$ with $N_f=2$



The same patterns persist for other channels.

#### BSM wishlist from the lattice

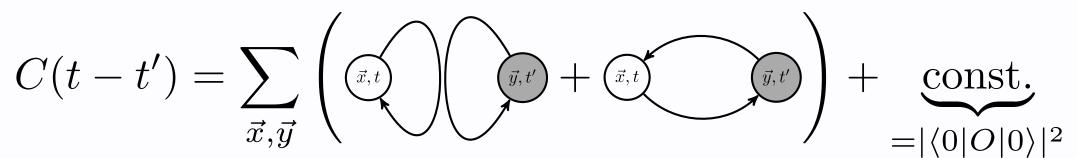
- Masses and decay constants of dark hadrons
- Scattering of dark pions:  $2\pi 
  ightarrow 2\pi$  and  $3\pi 
  ightarrow 2\pi$
- Applicability of  $\chi {\rm PT}$  and related EFTs
- Composite Higgs studies can be repurposed
  - Composite Higgs model usually allow SIMP DM

## Lattice Investigations:

Quantitative Insights

#### Calculating the meson correlator

- Evaluate diagrams in terms of fermion propagator  $D^{-1}$ 

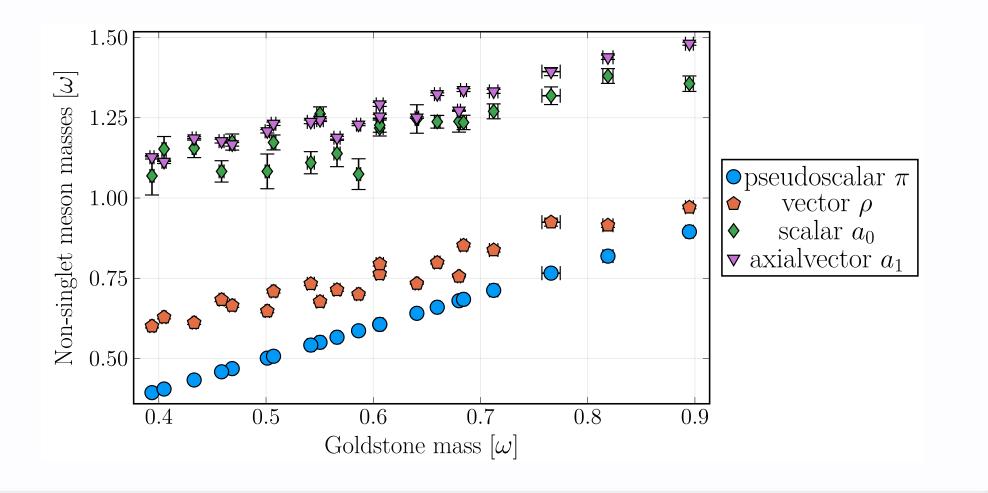


- Disconnected diagram (left) particularly challenging
   only appears for singlets (gluonic propagation)
- Constant term arises for singlets

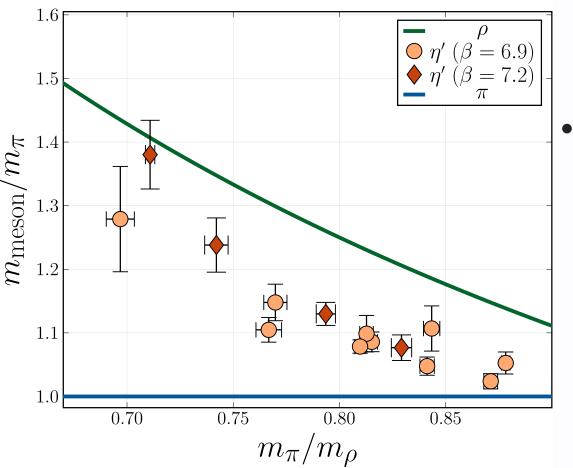
 $\circ$  vacuum term for  $\sigma$ , fixed topological charge for  $\eta'$ 

#### Bennett et. al. [1909.12662]

#### Non-singlet spectrum



The pseudoscalar and vector mesons are the lightest non-singlets.<sup>14</sup>



# The pseudoscalar singlet $\eta'$ is surprisingly light!

- Phenomenologically relevant:
  - $\circ \; m_
    ho > m_{\eta'} \;$  different from QCD
  - $\circ$  relevant low-energy dof
  - $\circ~\eta^{\prime}$  relevant for  $\pi\pi$  scattering
  - $\circ\,$  more accessible channels for

decays into SM

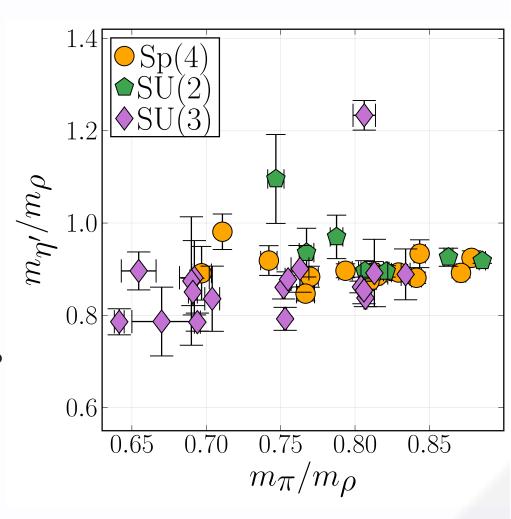
### Interesting! Is this surprising?

## Consider different theories:

• Large  $N_c\colon m_{\eta'}-m_\pi\propto N_f/N_c$  $\circ~N_f=2$  could be "small"  $\circ~N_c=4$  could be "large"

#### SU(2) and SU(3) comparison:

- Similarities:generic  $N_f = 2$  feature?
- QCD: strong  $N_f$  dependence
- Differences may arise  $m_\pi/m_
  ho o 0$ mass driven by flavour content!



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#### **Consequences for Dark Matter models**

- Mass hierarchies: limit  $\chi$ PT validity
  - $\circ$  inclusion of other states than  $\pi$  required, e.g.  $\eta'$  and ho
- Light unprotected state  $\eta' :$  decay into SM allowed
  - $\circ\,$  could be turned off at large N

Are these fermion masses phenomenologically relevant?

### Dark Matter Scattering on the Lattice

- Pions are in the 5-dimensional representations
- A two pion scattering is in one of three irreps  $5 imes 5 = 14 \oplus 10 \oplus 1$
- Corresponds to the usual QCD channels

 $\circ~14 \Leftrightarrow {\sf isospin}~I=2$  in QCD, e.g.  $\pi^+\pi^+$ 

 $\circ~10 \Leftrightarrow {\sf isospin}~I=1$  in QCD, e.g.  $\pi\pi o 
ho$ 

 $\circ \ 0 \Leftrightarrow {\sf isospin} \ I = 0$  in QCD, e.g.  $\pi\pi o \sigma/f_0$ 

## Scattering information from the lattice

- Scattering phase shift  $\delta_0(p)$  from finite volume energy

$$an(\delta_0(q))=rac{\pi^{rac{3}{2}}q}{\mathcal{Z}_{00}^{ec 0}(1,q^2)}, \quad q=p^*rac{L}{2\pi} \ \cosh\left(rac{E_{\pi\pi}}{2}
ight)=\cosh(m_{\pi\pi})+2\sin\left(rac{p^*}{2}
ight)^2$$

- Low-velocity behaviour: Scattering length
  - $\Rightarrow$  relation between  $\pi\pi$  energy  $E_{\pi\pi}$  and  $m_{\pi}$  on a lattice  $^{[1]}$

$$\frac{\delta E_{\pi\pi}}{m_{\pi}} = \frac{4\pi m_{\pi} a_0}{(m_{\pi}L)^3} \left( 1 + c_1 \frac{m_{\pi} a_0}{m_{\pi}L} + c_2 \left( \frac{m_{\pi} a_0}{m_{\pi}L} \right)^2 \right)$$

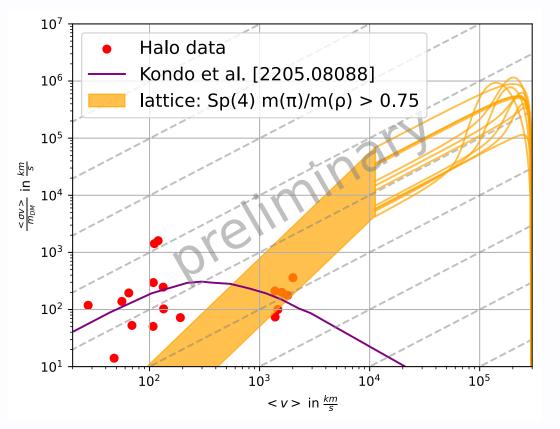
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[1] Dengler et.al. [2311.18549] see also Arthur et. al. [1412.4771] for SU(2) Blum et.al. [2301.09286] for SU(3)

#### 0.0 -0.2' 0.4– ש00ש -0.6 LO EFT $\beta = 6.90$ -0.8 $\beta = 7.05$ $\beta = 7.20$ -1.0 2 4 6 0 $\frac{m_{\pi}}{f_{\pi}}$

# First investigation of isospin-2 scattering

- repulsive  $\pi\pi$  interaction
- few lattice energy levels
   available ⇒ systematics
- finite volume effects present
- roughly matches ChiPT



# First investigation of isospin-2 scattering

- phase shift  $\delta(p)$  gives velocity dependence  $\langle \sigma v \rangle$
- No velocity dependence in isospin-2 channel
- Overall scale chosen to match low velocity behaviour

#### Summary

- Full light hadron spectrum of two-flavour Sp(4)
  - $\circ$  surprisingly light  $\eta'$
  - input for EFTs: masses and decay constants
  - $\circ$  first determination of isospin-2  $\pi\pi$  scattering

#### Outlook

- Full scattering analysis of  $2\pi o 2\pi$  and  $3\pi o 2\pi$  $\circ$  velocity dependence from strong resonances?
- Better understanding of singlets and scattering states
- Singlet spectroscopy closer to the chiral limit

## Thank you